

## (A Constituent college of Jomo Kenyatta University of Agriculture \& Technology)

## SCHOOL OF PURE AND APPLIED SCIENCE

END OF SEMESTER EXAMS SEMESTER 1 2015/2016
SMB 0101 ALGEBRA AND BUSINESS MATHEMATICS

## CLASS: CERTIFICATE IN BRIDGING MATHEMSTICS

TIME 2hrs

Instructions; Answer question ONE and any other TWO questions

1. (a) solve the following simultaneous equation

$$
\begin{aligned}
x+2 y-3 z & =10 \\
2 x-y+2 z & =-1 \\
3 x+2 y+z & =6
\end{aligned}
$$

[6mks]
(b)The $20^{\text {th }}$ term of an arithmetic sequence is 60 and the $16^{\text {th }}$ term is 20 . Find the first term and the common difference.
[4marks]
(c) Solve the equation $2 x^{2}+5 x=3$ by completing square method.
(d) Given that $\frac{D}{d}=\sqrt{\frac{f+p}{f-p}}$ make p the subject of the formula
(e) Find the value of $x$ in the equation

$$
4^{3 x-2}=26^{x+1}
$$

[4marks]
(f)The determinant of the matrix below is 6 , find the value of $x$.
$\left[\begin{array}{cc}X & X \\ 4 & 2 X\end{array}\right\rceil$
(4marks)
(d) In how many ways can a 3 digits number can be formed from 1,2,3,4 and 5?
2. (a) Solve the following using matrix method:

$$
\begin{align*}
& 4 x-3 y=18 \\
& x+2 y=-1 \tag{6marks}
\end{align*}
$$

(b) The following is geometric series $9+3+1+\frac{1}{3}+\ldots \ldots \ldots$, find the sum of all the terms i.e. upto infinity.
(c) Given that y varies inversely as x and that when $\mathrm{y}=6, \mathrm{x}=44$ find;
(i) equation connecting $x$ and $y$
(ii) y when $\mathrm{x}=2$
(d) In how many ways can a committee of 4 people be chosen from 7 people?
(e) Given that $\mathrm{I}=\mathrm{PV}^{\mathrm{n}}$ make n the subject of the formula.
3. (a)The sum of the first 20 terms of an arithmetic series is $7 \frac{1}{2}$. If the third term of the series is 2 , find the sum of the first 13 terms.
(b) The matrix below is singular find the unknown.
$\left[\begin{array}{cc}4 x & 2 \\ 5 & 2\end{array}\right]$
(c) Find the value of $x$ in the equation; $\log (x-1)+\log (x+1)=2 \log (x+2)$
(d) The value of a house was Ksh 2560000 three years ago. If it appreciates at the rate of $3 \%$ per annum what will be the value of the house next year.
(e) A trader sold an item at ksh 1350, this was after allowing a discount of $10 \%$. If he did not give the discount he would have made a profit of $20 \%$, how much did the trader buy the item? 3mks
4. (a) Solve the following equation using factorization method $x^{2}-x-6=0$
(b) Solve the following simultaneous equation using substitution method:

$$
\begin{gather*}
4 x-3 y=18 \\
x+2 y=-1 \tag{3marks}
\end{gather*}
$$

(c) John was collected a total Ksh 190 being offering in Sunday school on certain Sunday, there were twice 10 shillings coins as many as 20 shillings coin, 5 shillings coins exceeded 20 shillings coin by one coin while 10 shillings coin were more than 1 shilling coin by 3 coins. Find number of coins per each denomination.
(d) Expand the following $(1+x)^{7}$ up to the term with $x^{3}$ and use your expansion to estimate $(1.05)^{7}$
(e) Simplify the following;

$$
\frac{\log _{16} 2-\log _{4} 64}{4 \log _{8} 2-3 \log _{27} 3}
$$

5. (a) A vehicle was depreciating at the rate of $12 \%$ annually, if the value of the vehicle is Ksh 524880 today what was the value of the vehicle 4 years ago.
(b) Find the value of x in the equation; $\mathrm{X}^{1.5}=14.91$
(c) In how many ways would six people sit on a bench?
(d) Given that y varies directly as x and when $\mathrm{x}=2, \mathrm{y}=3$. Find y when $\mathrm{x}=12$. ( 3 mks )
(e) Mr. john paid a certain item Ksh 580 which was inclusive of $16 \%$ V.A.T., what the price of the item before tax.
(f)Find $\left[\begin{array}{lll}5 & -2 & 4 \\ 2 & -3 & 7\end{array}\right] \times\left[\begin{array}{cc}1 & 3 \\ -5 & 2 \\ 4 & 6\end{array}\right]$ (3mks)
(g) Given the ratio of $a$ to $b$ is $2: 3$ and the ratio of $b$ is to $c$ is $4: 5$ and the ratio of $c$ tod is $1: 4$. Find the ratio of a tod.
