



# EMBU UNIVERSITY COLLEGE

(A Constituent College of the University of Nairobi)

2015/2016 ACADEMIC YEAR

FIRST SEMESTER EXAMINATION

THIRD YEAR EXAMINATION FOR THE DEGREE OF BACHELOR OF SCIENCE

SPH 201: MECHANICS II

DATE: DECEMBER 7, 2015

TIME: 14:00-16:00

## INSTRUCTIONS:

You may use the following constants:

Density of the earth,  $\rho = 5.51 \times 10^3 \text{ kg/m}^3$

Gravitational constant  $G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$

Gravitational acceleration,  $g = 10 \text{ m/s}^2$

**Answer Question ONE and ANY Other TWO Questions.**

## QUESTION ONE

- a) Using the kinematics of Simple Harmonic motion show that  $\omega = 2\pi f$  (5 marks)
- b) Using the equation of simple harmonic motion derive the equation for the velocity and acceleration of the a particle in simple harmonic motion in terms of velocity and acceleration amplitudes. (6 marks)
- c) The force acting on a particle in simple harmonic motion oscillator is given by the expression  $F = -kx\hat{i}$
- i.) Prove that the force is conservative (2 marks)
- ii.) Find the potential energy of the oscillator (3 marks)
- d) A coupled oscillator has two equal masses  $m$  connected by springs having equal spring constants  $k$  as shown in the figure below.



The masses are free to slide on a frictionless table AB. The walls A and B to which the ends of the springs are attached are fixed

- i.) Set up the differential equations for the motion (5 marks)
- ii.) Find the normal frequency for the system (4 marks)
- e) State the three Keplers laws of planetary motion (3 marks)
- f) Determine the force between two electrons separated by a distance of 0.1mm (3 marks)

### **QUESTION TWO**

- a) Derive the formulae for the period of a simple pendulum (8 marks)
- b) A 200-g block connected to a light spring for which the force constant is 5.00 N/m is free to oscillate on a horizontal, frictionless surface. The block is displaced 5.00 cm from equilibrium and released from rest. Compute:
  - i) The period of its motion (3 marks)
  - ii) The maximum velocity of the block (3 marks)
  - iii) Express the position, speed and acceleration as a function of time (6 marks)

### **QUESTION THREE**

- a) Show that for a spring in simple harmonic motion the period of oscillation is given by

equation  $T = 2\pi\sqrt{\frac{m}{k}}$  (8 marks)

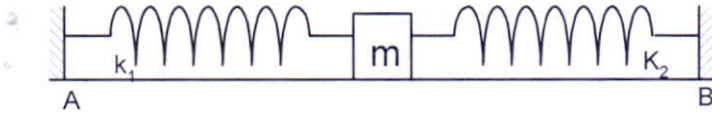
- b) The equation of a wave as time dependent along the x-direction is given by

$x(t) = 4.00\text{Cos}(\pi t + 0.25\pi)$  . Determine:

- i.) The amplitude (1 mark)
- ii.) The frequency f of the vibrating particles (3 marks)
- iii.) The phase and the Phasor when t=1 sec (2 marks)
- iv.) Calculate the velocity and the acceleration of the wave at any time. (6 marks)

#### QUESTION FOUR

- a) The figure below shows a mass  $m$  which is on a frictionless table connected to fixed points A and B by two springs of natural length, of negligible mass and spring constants  $K_1$  and  $K_2$  respectively.



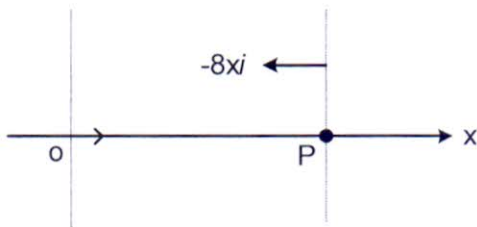
The mass  $m$  is displaced horizontally and then released. Prove that the period of

oscillation is given by the equation  $T = 2\pi \sqrt{\frac{m}{k_1 + K_2}}$  (7 marks)

- b) On the same axes sketch a graph of potential energy, kinetic energy and the total mechanical energy of a particle in simple harmonic motion for one complete oscillation. (5 marks)
- c) A 0.5kg cart connected to a light spring for which the force constant is 20.0N/M oscillates on a horizontal frictionless air track.
- Calculate the total energy of the system and the maximum speed of the cart if the amplitude of the motion is 3.00cm (5 marks)
  - What is the velocity of the cart when the position is 2.00cm? (3 marks)

#### QUESTION FIVE

- a) A particle of mass 2 moves away along the  $x$  axis attracted towards origin  $O$  by a force whose magnitude is equal to  $8x$  as shown in the figure below.



If it is initially at rest, at  $x=20$  find:

- The differential equations and the initial conditions describing the motion of the particle (3 marks)

- ii.) The position of the particle at any time (3 marks)
  - iii.) The speed and the velocity of the particle at any time (4 marks)
  - iv.) The amplitude, period and frequency of the vibration (4 marks)
- b) Suppose that the particle P in question 5a) above also has a damping force whose magnitude is numerically equal to 8 times the instantaneous speed, find the position and the velocity of the particle at any time. (6 marks)

**--END--**