

EMBU UNIVERSITY COLLEGE (A CONSTITUENT COLLEGE OF THE UNIVERSITY OF NAIROBI)

SECOND SEMESTER EXAMINATIONS 2013/2014

SECOND SEMESTER EXAMINATION FOR THE DEGREE OF BACELOR OF SCIENCE

SPH 102: ELECTRICITY AND MAGNETISM I

DATE: APRIL 4, 2014

TIME: 2.00 - 4.00PM

INSTRUCTIONS:

ANSWER QUESTION ONE AND ANY OTHER TWO QUESTIONS.

CONSTANTS

Electronic charge, e

 $= 1.602 \times 10^{-19} \,\mathrm{C}$

Velocity of light, c

= 3.0 x 10⁸ m/s

1 eV

 $= 1.602 \times 10^{-19} \,\mathrm{J}$

Mass of electron, me

= 9.11 x 10⁻³¹ kg

Mass of proton, m_p

= 1.67 x 10^{-27} kg

Permittivity of free space, ϵ_0

 $8.85 \times 10^{-12} \,\mathrm{C}^2/\mathrm{Nm}^2$

Acceleration due to gravity, $g = 10 \text{ m/s}^2$

Density of water $= 1 \text{ g/cm}^3$

QUESTION ONE (30 MARKS):

- a) Two spheres charged with equal but opposite charges experience a force of 170.5 N when they are placed 20 mm apart in a medium of relative permeability 3. Determine the charge on each sphere.

 (3 marks)
- b) Show that the amount of work done in bringing a charge dq a unit distance in an electric field is equivalent to: $-W = \frac{1}{2}CV^2$. (3 marks)
- c) Three capacitors are connected in series across a 75 V supply. The voltages across them are 20 V, 25 V and 30 V respectively and the charge on each is $3 \times 10^{-3} C$. Find the capacitance of the combination. (3 marks)
- d) Two rails of a railway track insulated from each other and the ground are connected to a millivolt-meter. What would be the reading of the millivolt meter when the train travels at a speed of $180 \, km/h$ along the track, given that the horizontal component of earth's magnetic field is $0.2 \, x \, 10^{-4} \, Wb/m^2$ and the rails are separated by 1 meter. (4 marks)
- e) An air cored solenoid has 300 turns, its length is 25 cm and its cross-section is $3 cm^2$. Calculate its self-inductance. (3 marks)
- f) Consider a unit North Pole of strength, m of one weber placed at a point, a distance r, in a magnetic field. Show using unit vector that the magnetic field intensity is given

by
$$\vec{H} = \frac{m}{4\pi\mu\vec{r}^3}N/Wb$$
 (3 marks)

g) A galvanometer which requires a current of I_g for full-scale deflection and a galvanometer resistance G is intended for conversion to an ammeter. Taking S to be the shunt resistance to be used, show that: -

$$S = G(\frac{I_g}{1 - I_g}) \tag{4 marks}$$

h) Considering a point A in an electric field whose intensity is \vec{E} , a unit positive charge is placed at this point and then moved to another point B at a distance dx from point A. show that the electric field intensity \vec{E} is equal to the rate of change of potential with distance.

(4 marks)

i) Explain three factors upon which capacitance of a capacitor depend on. (3 marks)

QUESTION TWO (20 MKS)

- a) Find the capacitance of coaxial cylinder with insulator of permeability ϵ_r , Q is the charge in coulombs per meter and that the potential difference of V is applied between. (7 marks)
- b) Three A, B and C charges of $\frac{2}{3} \times 10^{-9} C$, $\frac{8}{3} \times 10^{-9} C$ and $\frac{10}{3} \times 10^{-9} C$ respectively are placed at three corners of an equilateral triangle of side 10 cm. Find the resultant and direction force on the charge of $\frac{10}{3} \times 10^{-9} C$.

(13 marks)

QUESTION THREE (20 M ARKS)

a) The resistance of a field coil measures $55\,\Omega$ at $25^{0}C$ and $65\,\Omega$ at $75^{0}C$. Find the temperature coefficient of the conductor at $0^{0}C$.

- b) Two points charges of 12×10^{-10} C and 8×10^{-10} C are 10 cm apart. Find the work done in bringing the charges 4 cm closer. (7 marks)
- c) Show that the magnetic flux density at a distance x from a long straight wire is given by:

$$-\vec{B} = \frac{\mu_0 I}{2\pi R} \qquad (5 \text{ marks})$$

QUESTION FOUR (20 MARKS)

- a) A wire carrying a current of 100 amperes is bent into the form of a circle of radius 5.08 cm. Calculate the flux density at the center of the coil and flux density perpendicular to the plane of the coil at a distance of 12 cm from the coil. (6 marks)
- b) The figure below shows two batteries in opposition to each other. One has an emf of 6V and internal resistance r_1 of 2Ω and the other an emf E_2 of 4V and internal resistance r_2 of 8Ω . Calculate the potential difference V_{xy} across xy. (8 marks)

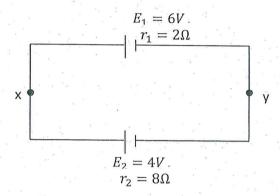


Figure 4.1: Fig. 4.1

c) A long straight conductor x carrying a current of 2A is placed parallel to a short conductor y of length 0.05 m carrying a current of 3A. The two conductors are 0.10 m apart. Calculate the flux density due to x at y and the approximate force on y. (6 marks)

QUESTION FIVE (20 MARKS)

ABCD is a rectangle. At corners B, C and D of the rectangle is placed charges+ 10×20^{-12} C, -20×10^{-12} C and $+10 \times 10^{-12}$ C respectively. Calculate the potential at the fourth corner A. the side AB=4cm and BC=3cm. (10 marks)

a) A potential difference of 20KV is applied to a parallel plate capacitor with a plate area of 0.01m^2 . The plates are separated by a dielectric 2mm thick. The capacitance of the capacitor is $2 \times 10^{-4} \mu F$. Find:

- i.) Total electric flux. (2)
- ii.) Potential gradient. (2)
- iii.) Relative permeability of the medium. (6)
- iv.) Energy stored. (3)

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