

# **EMBU UNIVERSITY COLLEGE**

(A Constituent College of the University of Nairobi)

#### 2015/2016 ACADEMIC YEAR

#### SECOND SEMESTER EXAMINATION

# SECOND YEAR EXAMINATION FOR THE DEGREE OF BACHELOR OF ECONOMICS SMA 201: CALCULUS II

**DATE: APRIL 12, 2016** 

TIME: 08:30-10:30

**INSTRUCTIONS:** Answer Question ONE and ANY Other TWO Questions.

#### **QUESTION ONE**

a) Solve for x:  $\ln(2 - \sin^2 x) = 0$ ,  $0 \le x \le 360^{\circ}$  (4 Marks)

b) Determine whether the series  $3 + 2 + \frac{4}{3} + \frac{8}{9} + \cdots$  is convergent or divergent. If it is convergent, determine its sum. (4 Marks)

c) Using the definition of a definite integral as the limit of a Riemann sum, prove that

$$\int_{3}^{4} (x^2 + 2)dx = 14\frac{1}{3}$$
 (6 Marks)

d) Evaluate the following integrals:

(i) 
$$\int \left(x^2 - 5\sqrt{x} + \frac{3}{x^2}\right) dx$$
 (2 Marks)

(ii) 
$$\int_0^1 x^2 (1 + 2x^3)^5 dx$$
 (4 Marks)

e) Using integration by parts, evaluate  $\int x^3 \ln x \, dx$  (3 Marks)

f) Determine the area of the region between the curve  $y = 27 - 3x^2$  and the x-axis. (4 Marks)

g) Evaluate the improper integral  $\int_0^\infty e^{-3x} dx$  (3 Marks)

# **QUESTION TWO**

a) Evaluate the following integrals:

(i) 
$$\int \frac{dx}{\sqrt{2x+1}}$$
 (3 Marks)

(ii) 
$$\int_0^1 x^2 e^x dx$$
 (4 Marks)

$$(iii) \int \frac{2x+3}{x^2-9} dx$$
 (4 Marks)

- b) If the marginal revenue for a commodity is  $9 6x^2 + 2x$  determine the total revenue and demand function (4 Marks)
- c) The marginal cost function of manufacturing x units of a commodity is  $6 + 10x 6x^2$ .

  Determine the total cost and average cost, given that the total cost of producing 1 unit is Shs.

  15. (5 Marks)

# **QUESTION THREE**

- a) Evaluate the integral  $\int \frac{(1-5x)dx}{\sqrt[5]{10x^2-4x+7}}$  (4 Marks)
- b) If the demand and supply functions under pure competition are given by  $p_d(x) = 16 x^2$  and  $p_s(x) = 2x^2 + 4$ , respectively, determine the consumer's surplus and producer's surplus at the market equilibrium price. (16 Marks)

# **QUESTION FOUR**

- a) Use the partial fraction decomposition technique to evaluate  $\int_{1}^{2} \frac{4x^{2}-7x-12}{x(x+2)(x-3)} dx$  (11 Marks)
- b) Find the area of the region bounded by the curves  $y = x^2 5$  and  $y = 3 x^2$  (9 Marks)

#### **QUESTION FIVE**

a) Evaluate the following integrals:

(i) 
$$\int \left(\sqrt[3]{x} - \frac{1}{x} + \sin\theta\right) dx$$
 (4 Marks)

(ii) 
$$\int \frac{x^2 dx}{(4-x^3)^{3/2}}$$
 (4 Marks)

- b) Evaluate the improper integral  $\int_2^5 \frac{dx}{\sqrt{x-2}}$  (4 Marks)
- c) Determine the area of the region enclosed between the curves  $y = x^2$  and  $y = x^2 + 2x + 3$  from x = 1 to x = 2.5 (8 Marks)

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